

Derivada del producto de dos polinomios

$$1) y = (-3x^2 - 2x + 3)(-4x^2 - 6x - 2)$$

$$\begin{aligned}y' &= (-6x - 2)(-4x^2 - 6x - 2) + (-3x^2 - 2x + 3)(-8x - 6) = \\ &= 24x^3 + 44x^2 + 24x + 4 + 24x^3 + 34x^2 - 12x - 18 \\ &= 48x^3 + 78x^2 + 12x - 14\end{aligned}$$

$$2) y = (4x^2 - 6x - 5)(4x^2 + 5x - 3)$$

$$\begin{aligned}y' &= (8x - 6)(4x^2 + 5x - 3) + (4x^2 - 6x - 5)(8x + 5) = \\ &= 32x^3 + 16x^2 - 54x + 18 + 32x^3 - 28x^2 - 70x - 25 \\ &= 64x^3 - 12x^2 - 124x - 7\end{aligned}$$

$$3) y = (5x^2 - 5)(2x^2 - 4x - 5)$$

$$\begin{aligned}y' &= 10x(2x^2 - 4x - 5) + (5x^2 - 5)(4x - 4) = \\ &= 20x^3 - 40x^2 - 50x + 20x^3 - 20x^2 - 20x + 20 \\ &= 40x^3 - 60x^2 - 70x + 20\end{aligned}$$

$$4) y = (-4x^2 - 6x - 6)(-x^2 + 2x + 1)$$

$$\begin{aligned}y' &= (-8x - 6)(-x^2 + 2x + 1) + (-4x^2 - 6x - 6)(-2x) = \\ &= 8x^3 - 10x^2 - 20x - 6 + 8x^3 + 4x^2 - 12 \\ &= 16x^3 - 6x^2 - 20x - 18\end{aligned}$$

$$5) y = (-6x^2 - 5x - 5)(4x^2 + 5x - 5)$$

$$\begin{aligned}y' &= (-12x - 5)(4x^2 + 5x - 5) + (-6x^2 - 5x - 5)(8x + 5) = \\ &= -48x^3 - 80x^2 + 35x + 25 - 48x^3 - 70x^2 - 65x - 25 \\ &= -96x^3 - 150x^2 - 30x\end{aligned}$$

$$6) y = (3x^2 + 2x + 4)(x^2 + x + 4)$$

$$\begin{aligned}y' &= (6x + 2)(x^2 + x + 4) + (3x^2 + 2x + 4)(2x + 1) = \\ &= 6x^3 + 8x^2 + 26x + 8 + 6x^3 + 7x^2 + 10x + 4 \\ &= 12x^3 + 15x^2 + 36x + 12\end{aligned}$$

$$7) y = (-5x^2 + 5x - 3)(x^2 + 5)$$

$$\begin{aligned}y' &= (-10x + 5)(x^2 + 5) + (-5x^2 + 5x - 3)2x = \\ &= -10x^3 + 5x^2 - 50x + 25 - 10x^3 + 10x^2 - 6x \\ &= -20x^3 + 15x^2 - 56x + 25\end{aligned}$$

$$8) y = (3x^2 + 4x - 1)(5x^2 + 6x - 3)$$

$$\begin{aligned}y' &= (6x + 4)(5x^2 + 6x - 3) + (3x^2 + 4x - 1)(10x + 6) = \\ &= 30x^3 + 56x^2 + 6x - 12 + 30x^3 + 58x^2 + 14x - 6 \\ &= 60x^3 + 114x^2 + 20x - 18\end{aligned}$$

$$9) y = (-x^2 + 5x - 3)(-4x^2 - x - 4)$$

$$\begin{aligned}y' &= (5 - 2x)(-4x^2 - x - 4) + (-x^2 + 5x - 3)(-8x - 1) = \\ &= 8x^3 - 18x^2 + 3x - 20 + 8x^3 - 39x^2 + 19x + 3 \\ &= 16x^3 - 57x^2 + 22x - 17\end{aligned}$$

$$10) y = (-5x^2 + 3x + 2)(5x + 3)$$

$$\begin{aligned}y' &= (-10x + 3)(5x + 3) + (-5x^2 + 3x + 2)5 = \\ &= -50x^2 - 15x + 9 - 25x^2 + 15x + 10 \\ &= -75x^2 + 19\end{aligned}$$

